

Review for Logs Test

Solve each equation.

1) $6^{-3x} = 6^{2x}$

$$\begin{array}{r} -3x = 2x \\ +3x \quad +3x \\ \hline 0 = 5x \end{array} \rightarrow x=0$$

3) $8^{-3n} = 16^{-n-3}$

$$(2^3)^{-3n} = (2^4)^{-n-3}$$

$$-9n = -4n - 12$$

$$-5n = -12$$

$$n = \frac{12}{5}$$

5) $4^{-3v} = \frac{1}{64}$

$$4^{-3v} = 4^{-3}$$

$$-3v = -3$$

$$v = 1$$

2) $2^{-2n} = 32$

$$2^{-2n} = 2^5$$

$$-2n = 5$$

$$n = 5/2$$

4) $4^{2x+3} = 64$

$$4^{2x+3} = 4^3$$

$$2x+3 = 3$$

$$2x = 0$$

$$x = 3/2$$

6) $5^{3x} = 625$

$$5^{3x} = 5^3$$

$$3x = 3$$

$$x = 1$$

Solve each equation. Round your answers to the nearest ten-thousandth.

7) $17^a = 27$

$$\log_{17} 27 = a$$

$$\frac{\log 27}{\log 17} = a$$

$$a = 1.1633$$

8) $e^b = 63$

$$\ln e^b = \ln 63$$

$$b = 4.1431$$

9) $10^{9x} = 70$

$$\log_{10} 70 = 9x$$

$$\frac{\log 70}{\log 10} = 9x$$

$$1.8451 = 9x$$

$$0.2050 = x$$

10) $7^{x+7} = 67$

$$\log_7 67 = x+7$$

$$\frac{\log 67}{\log 7} = x+7$$

$$2.1608 = x+7$$

$$-4.8392 = x$$

11) $18^{k-4} - 6 = 71$

$$18^{k-4} = 77$$

$$77 = k-4$$

$$\log_{18} 77 = k-4$$

$$\frac{\log 77}{\log 18} = k-4$$

$$1.5029 = k-4$$

$$5.5029 = k$$

12) $e^{5n} + 8 = 31$

$$e^{5n} = 23$$

$$5n = \ln(23)$$

$$5n = 3.1354$$

$$n = 0.6271$$

1. Adam invested \$400 in a CD that pays out 5.5% percent interest compounded monthly. What is the amount after 11 years?

$$A = A$$

$$P = 400$$

$$r = 0.055$$

$$n = 12$$

$$t = 11$$

$$A = 400 \left(1 + \frac{0.055}{12}\right)^{12 \cdot 11}$$

$$A = \$731.49$$

2. Sarah has a savings bond that will be worth \$15,000 in 10 years. The interest rate of the bond is 8.25% that is compounded semi-annually. Find the present value of the bond.

$$A = 15000$$

$$P = x$$

$$r = 0.0825$$

$$n = 2$$

$$t = 10$$

$$15000 = P \left(1 + \frac{0.0825}{2}\right)^{20}$$

$$\$6683.30 = P$$

3. \$1000 is invested at 4.7% in an account that is compounded continuously. How long will it take for the account to double?

$$A = 2000$$

$$P = 1000$$

$$r = 0.047$$

$$n = e$$

$$t = t$$

$$2000 = 1000 e^{0.047t}$$

$$2 = e^{0.047t}$$

$$\ln 2 = 0.047t$$

$$14.75 \text{ years} = t$$

4. How much money did Jenifer invest 10 years ago in an account that has a rate of 6% compounded continuously if he has a current balance of \$4008.66?

$$A = 4008.66$$

$$P = P$$

$$r = 0.06$$

$$t = 10$$

$$4008.66 = P e^{0.06(10)}$$

$$2200 = P$$

5. Tim invested \$5000 in a bond that has an interest rate of 7.65% compounded quarterly. The current value of the bond is \$6500. How long did Tom leave his money invested?

$$A = 6500$$

$$P = 5000$$

$$r = 0.0765$$

$$n = 4$$

$$t = t$$

$$6500 = 5000 \left(1 + \frac{0.0765}{4}\right)^{4t}$$

$$1.3 = \left(1 + \frac{0.0765}{4}\right)^{4t}$$

$$1.3 = (1.019)^{4t}$$

$$\log 1.3 = \log (1.019)^{4t}$$

$$\log 1.3 = 4t \log 1.019$$

$$13.819 = 4t$$

$$t = 3.5 \text{ years}$$

6. If \$1000 is invested in an account that is compounded continuously for 8 years, the account grows to \$3800. What would the interest rate be on the account?

$$A = 3800$$

$$P = 1000$$

$$r = r$$

$$n = e$$

$$t = 8$$

$$3800 = 1000 e^{8r}$$

$$3.8 = e^{8r}$$

$$\frac{\ln(3.8)}{8} = \frac{8r}{8}$$

$$r = 0.167$$

GROWTH AND DECAY:

7. The mice population is 15,000 and is decreasing by 13% each year. Write a formula for this situation. What will be the mice population after 2.5 years?

$$A = 15000(1 - 0.13)^{2.5}$$
$$A = \$10589.84$$

$$P = 15000$$

$$r = 0.13$$

$$t = 2.5$$

8. Teachers in Georgia are promised a 3% raise in yearly salary every year for the next 5 years. Write a formula for teachers' salaries. If a teacher is making \$62,000 now, how much will they be making in 5 years?

$$A = 62000(1 + 0.03)^5$$
$$A = \$53241.51$$

9. The number of mosquitoes at the beach has increased 42% every year since 1999. In 1999, there were 2,500 mosquitoes. Write a formula for this situation. How many mosquitoes would you predict were at the beach in 2020?

$$A = 2500(1 + 0.42)^{21}$$
$$A = 3944530 \text{ mosquitos}$$

10. The llama population has been growing by 2.5% every year. There are currently 1.08 million llamas in 2018. Write a formula for the llama population. Then use it to predict the population in the year 2027.

$$A = 1.08(1 + 0.025)^t$$
$$A = 1.08(1 + 0.025)^9 = 1.35 \text{ million llamas}$$

11. A new computer was purchased for \$1250. The value of the computer depreciates at a rate of 7.1% per year. Write a formula for the value of the computer. How much will the computer be worth in 4 years?

$$A = 1250(1 - 0.071)^t$$

$$A = 1250(1 - 0.071)^4 = \$931.05$$

12. A new car was purchased for \$51,999. The value of a new car of this model depreciates at a rate of 17% for year. Write a formula for the car's value. What will the value of the car be in 6 years?

$$A = 51,999(1 - 0.17)^t$$

$$A = 51,999(1 - 0.17)^6 = \$17000.57$$