

Final Exam Fall Practice Test

Date _____ Period _____

Name each polynomial by degree and number of terms.

1) $6x$

- A) fifth degree trinomial
- B) linear monomial
- C) constant monomial
- D) linear binomial

2) $6 - 9n^2$

- A) quadratic trinomial
- B) linear binomial
- C) cubic binomial
- D) quadratic binomial

Simplify each expression.

3) $(7x^2 + 3x^4 - 6) + (7x^2 + 4 + 4x^4)$

- A) $20x^4 + 14x^2 - 2$
- B) $13x^4 + 14x^2 - 2$
- C) $20x^4 + 12x^2 - 2$
- D) $7x^4 + 14x^2 - 2$

4) $(6x^2 + x + 4x^3) - (3x - 8x^2 - x^3)$

- A) $5x^3 + 14x^2 - 2x$
- B) $5x^3 + 22x^2 + 5x$
- C) $5x^3 + 14x^2 + 5x$
- D) $5x^3 + 30x^2 + 5x$

Find each product.

5) $(3n - 7)(7n - 5)$

- A) $21n^2 - 64n + 35$
- B) $21n^2 - 34n - 35$
- C) $12n^2 + 8n - 20$
- D) $5n^2 + 3n - 2$

6) $(4b + 4)(b^2 + 4b - 2)$

- A) $36b^3 - 12b^2 - 24$
- B) $30b^3 - 13b^2 + 3b + 1$
- C) $4b^3 + 20b^2 + 8b - 8$
- D) $5b^3 + 27b^2 - 54b + 14$

Simplify.

7) $(-5 - 4i) - (7 + i)$

- A) $-12 - 5i$
- B) $-13 - 4i$
- C) $-17 - 6i$
- D) $2 - 3i$

8) $(1 + 4i) + (2 - 5i)$

- A) $-3 - i$
- B) $1 + i$
- C) $3 - i$
- D) $-1 - 9i$

9) $(7 - 2i)(5 + 4i)$

- A) $27 - 38i$ B) $43 + 18i$
 C) $71 + 22i$ D) $23 + 14i$

10) $(4 - 8i)^2$

- A) 25 B) $-48 - 64i$
 C) 36 D) $-48 + 64i$

Perform the indicated operation.

11) $g(n) = n + 3$
 $h(n) = -2n + 1$
 Find $g(h(n))$

- A) $9n^2 - 6n - 3$ B) $-2n + 4$
 C) $-2n - 5$ D) $2n - 5$

12) $g(x) = 2x + 4$
 $h(x) = x^3 + 2$
 Find $g(x) - 3h(x)$

- A) $-x^3 + 6x - 10$
 B) $x^2 + 14x + 6$
 C) $-3x^3 + 2x - 2$
 D) $x^3 - 6x - 10$

Factor each completely.

13) $125a^3 + 27$

- A) $(5a + 3)^3$
 B) $(5a + 3)(5a - 3)^2$
 C) $(5a + 3)(25a^2 - 15a + 9)$
 D) $(5a - 3)(25a^2 + 15a + 9)$

14) $15k^3 + 40k^2 + 6k + 16$

- A) $(5k^2 - 2)(5k^2 + 8)$
 B) $(5k^2 + 2)(5k^2 - 8)$
 C) $(5k^2 - 2)(3k - 2)$
 D) $(5k^2 + 2)(3k + 8)$

Solve each equation by factoring.

15) $n^2 - 13n = -42$

- A) $\{-8\}$ B) $\{7, 6\}$
 C) $\{4, -7\}$ D) $\{-1, 0\}$

16) $2x^2 = 15x - 28$

- A) $\left\{\frac{7}{2}, 4\right\}$ B) $\left\{\frac{7}{2}, 2\right\}$
 C) $\left\{\frac{8}{5}, \frac{5}{7}\right\}$ D) $\left\{\frac{1}{5}, \frac{3}{2}\right\}$

Solve each equation by taking square roots.

17) $4n^2 - 4 = -32$

- A) $\{3i, -3i\}$ B) $\{3i\}$
C) $\{2, -2\}$ D) $\{i\sqrt{7}, -i\sqrt{7}\}$

Solve each equation with the quadratic formula.

18) $v^2 + 4v + 5 = 0$

- A) $\{2\sqrt{6}, -2\sqrt{6}\}$
B) $\{2\sqrt{2}, -2\sqrt{2}\}$
C) $\{-2 + i, -2 - i\}$
D) $\{\sqrt{2}, -\sqrt{2}\}$

Find all rational zeros. One zero has been given.

19) $f(x) = x^3 - 6x^2 + 3x + 10$; 2

- A) $\{-7, -1, 2\}$ B) $\{5, -1, -3\}$
C) $\{5, -1, 2\}$ D) $\{5, -3, 2\}$

Find all zeros.

20) $f(x) = 5x^3 + 5x^2 - 2x - 2$

- A) $\left\{-\frac{1}{3}, \frac{\sqrt{10}}{5}, -\frac{\sqrt{10}}{5}\right\}$
B) $\{0 \text{ mult. } 3\}$
C) $\left\{-1, \frac{\sqrt{10}}{5}, -\frac{\sqrt{10}}{5}\right\}$
D) $\left\{-\frac{1}{2}, \frac{\sqrt{10}}{5}, -\frac{\sqrt{10}}{5}\right\}$

21) $f(x) = 4x^3 + 20x^2 + 5x + 25$

- A) $\left\{-5, \frac{i\sqrt{30}}{5}, -\frac{i\sqrt{30}}{5}\right\}$
B) $\left\{-7, \frac{i\sqrt{5}}{2}, -\frac{i\sqrt{5}}{2}\right\}$
C) $\left\{-4, \frac{i\sqrt{5}}{2}, -\frac{i\sqrt{5}}{2}\right\}$
D) $\left\{-5, \frac{i\sqrt{5}}{2}, -\frac{i\sqrt{5}}{2}\right\}$

Write a polynomial function of least degree with integral coefficients that has the given zeros.

22) $-5, -2, 5$

- A) $f(x) = x^3 + x^2 - 25x - 50$
- B) $f(x) = x^3 + 2x^2 - 25x - 50$
- C) $f(x) = x^3 + 2x^2 - 29x - 50$
- D) $f(x) = x^3 - 25x - 50$

23) $5, -2i, 2i$

- A) $f(x) = x^3 - 5x^2 + 3x - 20$
- B) $f(x) = x^3 - 5x^2 + 4x - 19$
- C) $f(x) = x^3 - 5x^2 + 4x - 20$
- D) $f(x) = x^3 - 5x^2 + 4x - 25$

Divide.

24) $(b^3 - 5b^2 - 2b + 29) \div (b - 3)$

- A) $b^2 - 2b - 9 + \frac{7}{b-3}$
- B) $b^2 - 4b - 8 + \frac{6}{b-3}$
- C) $b^2 - 2b - 8 + \frac{7}{b-3}$
- D) $b^2 - 2b - 8 + \frac{5}{b-3}$

25) $(n^4 + 9n^3 - 5n - 50) \div (n + 9)$

- A) $n^3 - 2$
- B) $n^3 - 7 - \frac{10}{n+9}$
- C) $n^3 - 2 - \frac{6}{n+9}$
- D) $n^3 - 5 - \frac{5}{n+9}$

Simplify each expression.

26) $\frac{p^2 + 10p + 21}{p^2 + 17p + 70}$

- A) $\frac{p-8}{p+8}$
- B) $\frac{p+10}{p+3}$
- C) $\frac{p+3}{p+10}$
- D) $\frac{p-10}{2}$

27) $\frac{1}{x+9} \cdot \frac{x^2 + 11x + 10}{x+10}$

- A) $\frac{x+1}{x+9}$
- B) $\frac{x+9}{6x^2}$
- C) $\frac{3x^2}{x+7}$
- D) $6(x+3)$

$$28) \frac{12x^3 + 18x^2}{x+4} \div \frac{12x^3 + 18x^2}{x+2}$$

$$A) \frac{6}{x+1} \quad B) \frac{x+2}{x+4}$$

$$C) \frac{6}{x-7} \quad D) 8x$$

$$29) \frac{5x-3}{4x-4} - \frac{x-5}{4x-4}$$

$$A) \frac{2x+1}{2x-2} \quad B) \frac{7x+3}{4x-4}$$

$$C) \frac{2x+3}{5x+1} \quad D) \frac{-30x+15}{16x^2-32x+16}$$

$$30) \frac{4}{3m+3} + \frac{2}{m-2}$$

$$A) \frac{-4-m}{3(m+1)}$$

$$B) -\frac{4}{3(m+1)}$$

$$C) \frac{-3m+1}{3(m+1)}$$

$$D) \frac{10m-2}{3(m-2)(m+1)}$$

Solve each equation. Remember to check for extraneous solutions.

$$31) \frac{2a-6}{3a^2} = \frac{1}{a} + \frac{1}{3a}$$

$$A) \{-3, 0\} \quad B) \{-3\}$$

$$C) \{-4\} \quad D) \{6\}$$

$$32) \frac{1}{a^2-6a} = \frac{2}{a^2-6a} - \frac{1}{a}$$

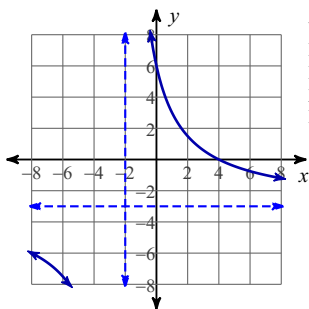
$$A) \left\{ \frac{4}{3} \right\} \quad B) \{-7\}$$

$$C) \{5\} \quad D) \{7\}$$

Identify the holes, vertical asymptotes, x and y-intercepts, horizontal asymptote, and domain of each. Then sketch the graph.

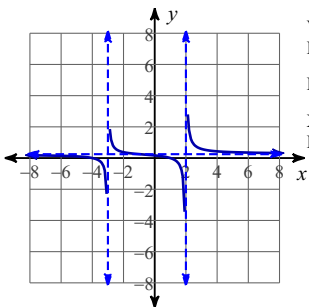
33) $f(x) = \frac{x + 2}{-3x + 12}$

A)



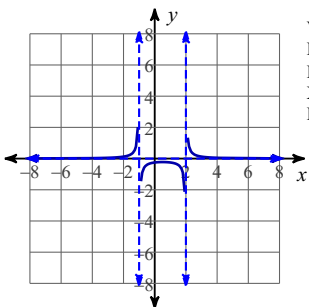
Vertical Asym.: $x = -2$
 Holes: None
 Horz. Asym.: $y = -3$
 X-intercepts: 4
 Domain:
 All reals except -2

B)



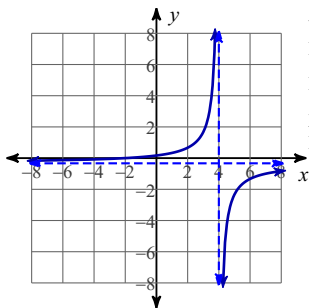
Vertical Asym.: $x = 2, x = -3$
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 Horz. Asym.: $y = \frac{1}{4}$
 X-intercepts: 1, -4
 Domain:
 All reals except 2, -3

C)



Vertical Asym.: $x = 2, x = -1$
 Holes: None
 Horz. Asym.: $y = 0$
 X-intercepts: None
 Domain:
 All reals except 2, -1

D)



Vertical Asym.: $x = 4$
 Holes: None
 Horz. Asym.: $y = -\frac{1}{3}$
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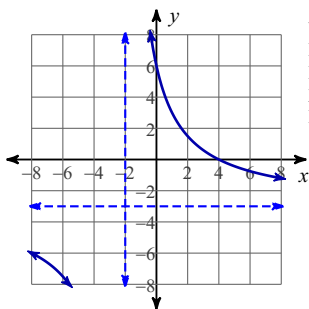
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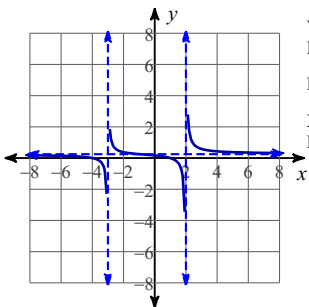
33) $f(x) = \frac{x+2}{-3x+12}$

A)



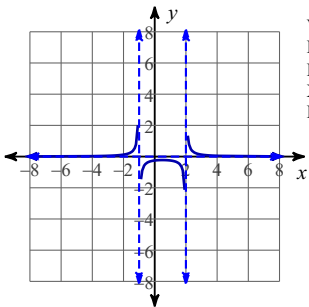
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 X-intercepts: 4
 Domain:
 All reals except -2

B)



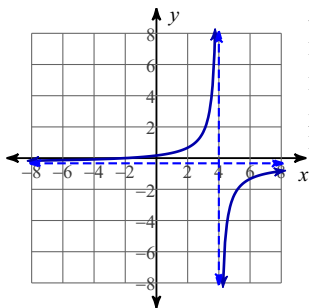
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 Holes: None
 Horz. Asym.: $y = \frac{1}{4}$
 X-intercepts: 1, -4
 Domain:
 All reals except 2, -3

C)



Vertical Asym.: $x = 2, x = -1$
 Holes: None
 Horz. Asym.: $y = 0$
 X-intercepts: None
 Domain:
 All reals except 2, -1

*D)



Vertical Asym.: $x = 4$
 Holes: None
 Horz. Asym.: $y = -\frac{1}{3}$
 X-intercepts: -2
 Domain:
 All reals except 4