

69. Which sequence of transformations maps $\triangle ABC$ to $\triangle RST$?

A. Reflect $\triangle ABC$ across the line $x = -1$. Then translate the result 1 unit down.
 B. Reflect $\triangle ABC$ across the line $x = -1$. Then translate the result 5 units down.
 C. Translate $\triangle ABC$ 6 units to the right. Then rotate the result 90° clockwise about the point $(1, 1)$.
 D. Translate $\triangle ABC$ 6 units to the right. Then rotate the result 90° counterclockwise about the point $(1, 1)$.

1

Side – Angle Inequalities

-If one side of a triangle is longer than another side, then the angle opposite the longer side is larger than the angle opposite the smaller side.

2

Ex. 1 Write the measurements of the angles in order from least to greatest.

Step 1. Write the sides in order from least to greatest.
 $AB < BC < AC$

Step 2. Write the angles opposite those sides.
 $\angle C < \angle A < \angle B$

3

If one angle of a triangle is larger than another angle, then the side opposite the larger angle is longer than the side opposite the smaller angle.

Ex. 2 Write the measurements of the sides in order from least to greatest.

Step 1. List the angles in order from least to greatest.
 $\angle X < \angle Z < \angle Y$

Step 2. Write the sides opposite those angles.
 $YZ < XY < ZX$

4

Right Triangles

In a right triangle, the hypotenuse is the side with the greatest measure.

5

7-4 Triangle Inequality Theorem

The Sum of the measure of any two sides of a triangle is greater than the third side.

6

Ex. 1 Determine if the three numbers can be measures of the sides of a triangle. If no, explain.

- a. 13, 28, 19
 Yes $\begin{array}{r} 13 \\ +19 \\ \hline 28 < 32 \end{array}$ ✓
- b. 9, 4, 4
 No $\frac{4}{8} < 9$
- c. 9, 7, 2
 No $\frac{7}{9} = 9$

7

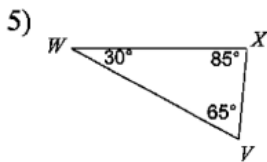
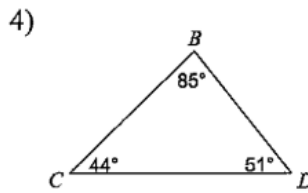
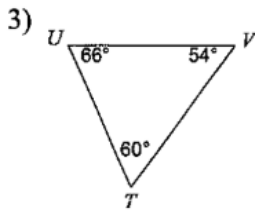
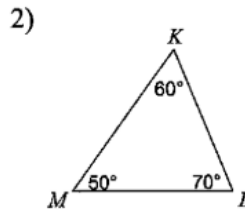
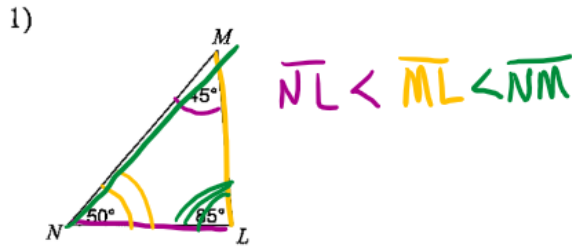
Ex. 2 If two sides of a triangle have the following measures, find the range of possible measures of the third side.

- low $< X <$ high
- a. 10, 7
 $\begin{array}{r} \text{low} \\ 10-7=3 \end{array}$ $\begin{array}{r} \text{high} \\ 10+7=17 \end{array}$
 $3 < X < 17$
- b. 18, 11
 $\begin{array}{r} \text{low} \\ 18-11=7 \end{array}$ $\begin{array}{r} \text{high} \\ 18+11=29 \end{array}$
 $7 < X < 29$

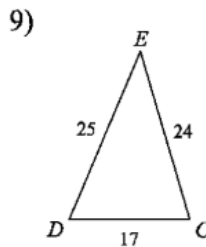
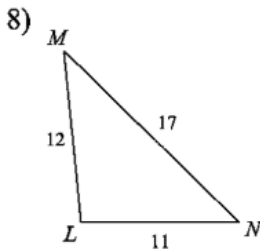
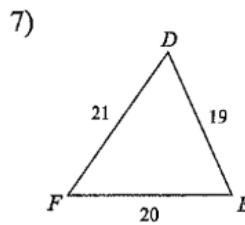
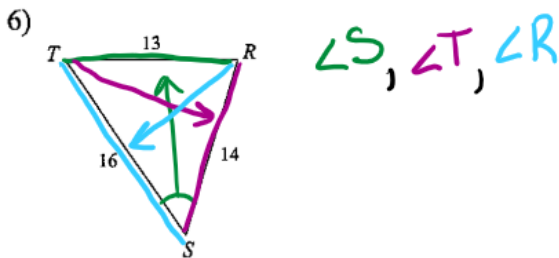
8

Triangle Inequality CW

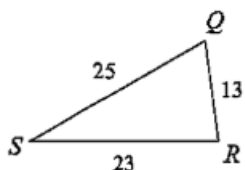
Order the sides of each triangle from shortest to longest.



Order the angles in each triangle from smallest to largest.



10)



State if the three numbers can be the measures of the sides of a triangle.

11) 14, 6, 8

$$\begin{array}{l} 8 \\ +6 \\ \hline 14 = 14 \end{array} \quad \text{No}$$

12) 11, 8, 6

13) 8, 12, 6

14) 5, 12, 7

15) 6, 12, 6

16) 4, 9, 6

17) 3, 12, 12

18) 11, 9, 4

19) 12, 4, 8

20) 9, 16, 7

Two sides of a triangle have the following measures. Find the range of possible measures for the third side.

21) 12, 12

22) 7, 6

23) 11, 11

24) 7, 8

25) 12, 10