

Compounded Interest

$$A = P \left(1 + \frac{r}{n}\right)^{nt} \quad A = P e^{rt}$$

(Compounded Continuously)

A = Final amount

P = Principal amount (starting amount)

r = rate (percentage as a decimal) $0.74\% \rightarrow 0.0074$

n = number of times compounds per year.

t = number of years (time)

n =	Compounding Periods
1	annually
2	semiannually
4	quarterly
12	monthly
52	weekly
365	daily
use other equation	Continuously

V

Bob is depositing \$400 in a savings account with 7% interest, compounded monthly. How much will be in the savings account in 10 years?

$$A = A$$

$$P = 400$$

$$r = 0.07$$

$$n = 12$$

$$t = 10$$

$$A = P(1 + \frac{r}{n})^{nt}$$

$$A = 400(1 + \frac{0.07}{12})^{120}$$

$$A = \$803.86$$

Janet started a bank account 12 years ago which paid 6% interest, compounded quarterly, and then forgot about it. She just remembered she had the account and checked the balance. She now has \$10,217.39. How much was her initial deposit? (4.12)

$$A = 10,217.39$$

$$P = P$$

$$r = 0.06$$

$$n = 4$$

$$t = 12$$

$$10,217.39 = P(1 + \frac{0.06}{4})^{48}$$

$$10,217.39 = P(2.04)$$

$$4999.999 = P$$

$$\$5000 = P$$

How long will it take for Robert to earn \$1200 on \$500 that earns 9% interest, compounded daily?

$$A = 1200$$

$$P = 500$$

$$r = 0.09$$

$$n = 365$$

$$t = t$$

$$\frac{1200}{500} = \frac{500(1 + \frac{0.09}{365})^{365t}}{500}$$

isolate base

$$(1.00024)^{365t} = 2.4$$

$$\log_{1.00024} 2.4 = 365t$$

$$\frac{\log 2.4}{\log 1.00024} = 365t \rightarrow 3550.95 = 365t$$

$$9.73 = t$$

Michael decides to invest his graduation money (\$2000) in a money market account which pays 7.2%, compounded continuously.

$$A = Pe^{rt}$$

How much will he have in 5 years?

$$A = A$$

$$P = 2000$$

$$r = 0.072$$

$$t = 5$$

$$A = 2000e^{(0.072)(5)}$$

$$A = 2866.66$$

When will the money double in value?

$$A = 4000$$

$$P = 2000$$

$$r = 0.072$$

$$t = t$$

$$\frac{4000}{2000} = \frac{2000e^{(0.072t)}}{2000}$$

$$2 = e^{(0.072t)}$$

$$\ln 2 = 0.072t$$

$$0.693 = 0.072t$$

$$9.63 \text{ years} = t$$

The following is the classwork and homework

Algebra II Support

Name:

$A = P\left(1 + \frac{r}{n}\right)^{nt}$, where P is the principal, r is the rate of interest, n is the type of compounding and t is the length of the investment.

$A = Pe^{rt}$, where P is the principal, r is the rate of interest, and t is the length of the investment.

1. Ron invested \$55,000 in a nine-year CD that pays out twelve percent compounded monthly. What is the amount after fifteen years?

2. Rick has a savings bond that will be worth \$8,220 in eight years. The interest rate of the bond is 5% that is compounded semiannually. Find the present value of the bond.

3. \$650 is invested at 5.2% in an account that is compounded continuously. How long would it take for the account to reach a balance of \$1000?

4. The number of tissue cells in a culture at the beginning of the experiment was 4300. If the cells split at a rate of $r = .12$, how many days will it take the culture to double? (Use $P = P_0e^{rt}$, where $P_0 = \#$ of cells at start, $P = \#$ of cells at end, $r =$ rate, $t =$ time in days.)

5. James has a savings bond that will be worth \$10,000 in seven years. The bond has an interest rate of 20% that is compounded semi-annually. Find the present value of the bond.

6. If \$2500 is invested in an account that is compounded continuously for 5 years, the account grows to \$3200. What would the interest rate be on this account?
